Imaging





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The "simple" microscope

















$$Mag|_{lateral} = \frac{\text{image distance}}{\text{object distance}}$$

$$\left| \text{Mag} \right|_{axial} = M^2$$

Thick lens from Melles Griot Optics Guide – link here: http://www.astro.caltech.edu/~lah/ay105/pdf/Fundamental-Optics.pdf essential optical layout of a modern microscope...



 $M_{total} = M_{objective} \times M_{eyepiece}$

Can you put the tube lens anywhere? Yes, but...



For building systems, and the lens spacing in infinity corrected (or other) systems, "telecentricity" is a nice design goal. If you look at the rays, you can see the central line are parallel to the optical axis, and this means When things move or blur, you don't see lateral shifts. Also, it means you see the same view, not A perspective view...













 $0.61 \cdot \lambda$ V NΑ mın

How do we see things?



CONTRAST

CONTRAST

Brightness of Specimen – Brightness of Background Brightness of Specimen + Brightness of Background



Brightness of Specimen – Brightness of Background Brightness of Specimen + Brightness of Background

0 Units



Brightness of Specimen – Brightness of Background Brightness of Specimen + Brightness of Background

0 Units

100 Units



Brightness of Specimen – Brightness of Background Brightness of Specimen + Brightness of Background



Brightness of Specimen – Brightness of Background Brightness of Specimen + Brightness of Background



Brightness of Specimen – Brightness of Background Brightness of Specimen + Brightness of Background



50 Units

50 Units

100 Units

Brightness of Specimen – Brightness of Background Brightness of Specimen + Brightness of Background



50 Units

50 Units

100 Units

Brightness of Specimen – Brightness of Background Brightness of Specimen + Brightness of Background

50 - 50 / 50 + 50 = 0

50 -100 / 50 + 100 = -0.33

How do you get contrast?

It depends on the sample, and the method of observation...

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- Brightfield
- Darkfield
- Phase Contrast
- Polarized Light
- DIC (Differential Interference Contrast)
- Fluorescence (and related techniques)

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Brightfield illumination





Ramon y Cajal



Brightfield illumination





Ramon y Cajal



Darkfield illumination



Direct light through sample at only oblique angles, and block direct light
Only light scattered, refracted, or reflected by sample makes it into the objective

•Bright object on dark background – sensitive to edges, outlines, and boundaries

•Sizes of features are not reliable



Fourier Transform... see https://en.wikipedia.org/wiki/Fourier_transform

$$\hat{f}\left(\xi
ight)=\int_{-\infty}^{\infty}f(x)~e^{-2\pi i x\xi}~dx,$$

Fourier transform pairs...

Image on left, FT on right. Spatial description – you see sine waves of intensity. The FT "image" shows you the frequency of the sine waves (two dots because + and - freq) *** Why don't you see the middle dot, like on my demo scope? Because in these pictures, I compute it for a "real" sine wave, meaning goes from -1 to 1, so average intensity is 0. In an Optical system, *some* light is always propagated, so you would see a middle dot.



Also note that this is just showing the Amplitude^2 of the transform, and doesn't show the phase. The phase part contains most of the information, re: where these frequency components match up in space... See next slide...



Matlab/imageJ

Under imagej/process/fft, can do ffts. What you see is the log scale image of the "power spectrum". That is it is the intensity of the particular frequency in the image. Each intensity would correspond to the coefficient in front of that freq in the Fourier decomposition of the image. The *phase* is NOT shown by default. Under fft options, you can have it displayed. Check it out....

Fourier Optics (thin lens)



Fourier Optics (thin lens)


Why does a lens do a transform? Well, from Maxwell's Eq. and A bunch of approximations, we see that that math works...

See http://web.mit.edu/2.710/Fall06/2.710-wk10-a-sl.pdf

Good ref book, but pretty technical https://www.macmillanlearning.com/college/us/product/Introduction-to-Fourier-Optics/p/1319119166



Why does NA affect resolution? If you imagine the diffraction of a small feature, this leads to wide angle scattering. If you don't capture those rays, you can't send them down your optical system. In terms of Fourier Optics, you don't capture the high frequency components in the fourier plane, so you are effectively doing a low-pass filter of the image.

Some Fourier transform pairs (graphical illustration)





Innovative Technology in the Public Interest"



Near-field distribution





Airy pattern





Transform pairs. Airy disk is the transform of a Circular disk. Other shapes have Different transforms...See next slide Nothing inherently fundamental about Airy disk in microscopy per se... it is just convenient to build circularly symmetric systems – both mechanically, and conceptually...

Rectangular aperture



Far field

Soft-edge apertures with different transition width



Diamond-shaped aperture

Corresponding far-field patterns:









	Field Plane	Fourier Plane
С	Field Amplitude, $E(x,y)$	$ ilde{E}(f_x,f_y)$
	Amplitude Point–Spread	Amplitude Transfer Function,
	Function, $h(x,y)$	$\tilde{h}(x,y)$
	Coherent Point–Spread Function	Coherent Transfer Function
	Point-Spread Function	Transfer Function
	PSF, APSF, CPSF	ATF, CTF
	$E_{image} = E_{object} \otimes h$	$\tilde{E}_{image} = \tilde{E}_{object} \times \tilde{h}$
Ι	Irradiance, $I(x, y)$	$\widetilde{I}(f_x, f_y)$
	Incoherent Point-Spread	Optical Transfer Function,
	Function, $H(x,y)$	$ ilde{H}(f_x,f_y)$
	Point-Spread Function	OTF
	PSF, IPSF	
		Modulation Transfer Function,
		$ \tilde{H} $
		MTF
		Phase Transfer Function, $\angle ilde H$
		PTF
	$I_{image} = I_{object} \otimes H$	$\tilde{I}_{image} = \tilde{I}_{object} \times \tilde{H}$

Nov. 2012

• Incoherent light, circular aperture

$$OTF(\rho') = \frac{2}{\pi} \left[a\cos(\rho') - \rho' \sqrt{1 - {\rho'}^2} \right]$$

where the normalized radial spatial frequency is given by, $\rho' = \rho / \rho_c$

and the cutoff frequency is given by,

$$\rho_c = \frac{D}{\lambda f} = \frac{1}{\lambda N} \text{ where } \begin{array}{l} D = \text{ aperture diameter} \\ f = \text{ focal length} \\ N = \text{ f-number} \\ \lambda = \text{ wavelength of light} \end{array}$$





Aberrations...



Chromatic Aberrations – because refractive index depends on Frequency (wavelength), lenses have different focal lengths for each color.





We fix that by making complex lenses that have multiple components, and we choose the shape and material so that the chromatic errors cancel out...

Apochromatic Objectives



Plenty of other aberrations too.

Wave front aberrations through order 6

Aberration name	Vector form	Algebraic form	j	m	n
Zero order					
Uniform piston	W_{000}	W_{000}	0	0	0
Second order					
Quadratic piston	$W_{200}(\vec{H} \ \vec{H})$	$W_{200}H^2$	1	0	0
Magnification	$W_{111}(ec{H} \mid ec{ ho})$	$W_{111}H\rho\cos(\phi)$	0	1	0
Focus	$W_{020}(\vec{ ho} \ \vec{ ho})$	$W_{020}\rho^2$	0	0	1
Fourth order					
Spherical aberration	$W_{040}(\vec{ ho} \ \vec{ ho})^2$	$W_{040} ho^4$	0	0	2
Coma	$W_{131}(\vec{H} \mid \vec{ ho})(\vec{ ho} \mid \vec{ ho})$	$W_{131}H\rho^3\cos(\phi)$	0	1	1
Astigmatism	$W_{222}(\vec{H} \mid \vec{ ho})^2$	$W_{222}H^2\rho^2\cos^2(\phi)$	0	2	0
Field curvature	$W_{220}(\vec{H} \ \vec{H})(\vec{\rho} \ \vec{\rho})$	$W_{220}H^2\rho^2$	1	0	1
Distortion	$W_{311}(\vec{H} \ \vec{H})(\vec{H} \ \vec{\rho})$	$W_{311}H^3\rho\cos(\phi)$	1	1	0
Quartic piston	$W_{400}(\vec{H} \ \vec{H})^2$	$W_{400}H^4$	2	0	0
Sixth order					
Oblique spherical aberration	$W_{240}(\vec{H} \ \vec{H})(\vec{\rho} \ \vec{\rho})^2$	$W_{240}H^2\rho^4$	1	0	2
Coma	$W_{331}(\vec{H} \ \vec{H})(\vec{H} \ \vec{\rho})(\vec{\rho} \ \vec{\rho})$	$W_{331}H^3\rho^3\cos(\phi)$	1	1	1
Astigmatism	$W_{422}(\vec{H} \ \vec{H})(\vec{H} \ \vec{\rho})^2$	$W_{422}H^4\rho^2\cos^2(\phi)$	1	2	0
Field curvature	$W_{420}(\vec{H} \ \vec{H})^2(\vec{\rho} \ \vec{\rho})$	$W_{420}H^4 ho^2$	2	0	1
Distortion	$W_{511}(\vec{H} \ \vec{H})^2 (\vec{H} \ \vec{\rho})$	$W_{511}H^5\rho\cos(\phi)$	2	1	0
Piston	$W_{600}(\vec{H} \ \vec{H})^3$	$W_{600}H^{6}$	3	0	0
Spherical aberration	$W_{060}(\vec{ ho} \ \vec{ ho})^3$	$W_{060} \rho^6$	0	0	3
Un-named	$W_{151}(\vec{H} \ \vec{\rho})(\vec{\rho} \ \vec{\rho})^2$	$W_{151}H\rho^5\cos(\phi)$	0	1	2
Un-named	$W_{242}(\vec{H} \ \vec{ ho})^2 (\vec{ ho} \ \vec{ ho})$	$W_{242}H^2\rho^4\cos^2(\phi)$	0	2	1
Un-named	$W_{333}(\vec{H} \ \vec{ ho})^3$	$W_{333}H^3\rho^3\cos^3(\phi)$	0	3	0



Through-focus images with pure astigmatism ($W_{222} = 2\lambda$)



4λ

0

 -4λ

 -3λ

1λ

 -7λ

J. Sasian, Introduction to aberrations in optical imaging systems, Fig. 7.6

Through-focus images with pure coma ($W_{131} = 2\lambda$)



0

 -4λ

J. Sasian, Introduction to aberrations in optical imaging systems, Fig. 7.5

1λ

 -3λ

 -7λ

Through-focus images with pure spherical ($W_{040} = 2\lambda$)



0

 -4λ

J. Sasian, Introduction to aberrations in optical imaging systems, Fig. 7.4

1λ

 -3λ

 -7λ



J. Sasian, Introduction to aberrations in optical imaging systems, Fig. 7.3

How deep can you go?



How deep can you go?







Adaptive optics via pupil segmentation for high-resolution imaging in biological tissues

Na Ji¹, Daniel E Milkie² & Eric Betzig¹

NATURE METHODS | VOL.7 NO.2 | FEBRUARY 2010 |

Slice severely aberrates the PSF

Image of a sub-resolution fluorescent object 50 µm within the slice



7 January 2008 / Vol. 16, No. 1 / OPTICS EXPRESS 67 Demixing light paths inside disordered metamaterials

I. M. Vellekoop¹, E. G. van Putten¹, A. Lagendijk^{1,2} and A. P. Mosk¹



High-speed scattering medium characterization with application to focusing light through turbid media

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High-speed scattering medium characterization with application to focusing light through turbid media

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Spatial Light Modulator (SLM)





Liquid crystal array

Microelectromechanical Mirror Array

Flexible control of the phase of light – programmable diffraction

SLM limitations?



Fundamentals of phase-only liquid crystal on silicon (LCOS) devices

Light: Science & Applications (2014) 3, e213; doi:10.1038/lsa.2014.94; published online 24 October 2014



$$E_{f}(x,y) = C \iint T_{-f}(x_{-f}, y_{-f}) \cdot \exp\left[-\frac{ik}{f}(x_{-f}x_{f} + y_{-f}y_{f})\right] dx_{-f} dy_{-f}$$





$$f(x,y) = C \iint T_{-f}(x_{-f}, y_{-f}) \cdot \exp\left[-\frac{ik}{f}(x_{-f}x_{f} + y_{-f}y_{f})\right] dx_{-f} dy_{-f}$$







Spatial Light Modulators: arbitrary shaping of light 3D



XZ view
CONTRAST



Brightness of Specimen - Brightness of Background Brightness of Specimen + Brightness of Background



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50 Units

0 Units



Brightness of Specimen – Brightness of Background Brightness of Specimen + Brightness of Background

50 Units

0 Units

100 Units



Brightness of Specimen – Brightness of Background Brightness of Specimen + Brightness of Background

50 Units



50 Units







Our job: measuring grass



Figure 10.1 Background signals.

Our job: measuring grass





Fluorescence







Principle of Fluorescence

- 1. Energy is absorbed by the molecule which becomes excited.
- 2. The electron jumps to a higher energy level.
- 3. Soon, the electron drops back to the ground state, emitting a photon (or a packet of light) the molecule is fluorescing.



Fluorescence Stoke's shift



- Fluorescence emission peak wavelength is red-shifted with respect to absorption peak wavelength
- This shift may vary typically from 5 to more than 100 nm, depending on the electronic structure of the molecule



Reaction Coordinate





TIME-DOMAIN LIFETIME MEASUREMENTS



Figure 4.37. Time and wavelength-dependent intensity decays of dimethyl-(4-pyren-1-yl-phenyl)amine (PyDMA) measured with a streak camera. Revised from [161].

In fluorescence, signal has inherent noise because you are counting discrete events – the arrival of photons. This noise is governed by Poisson statistics.

$$Signal = N$$
$$Std.Dev. = \sqrt{N}$$

Only 63% of the measurements are in the range

$$N \pm \sqrt{N}$$

Practical Implications?

To reliably detect activity with a S/N of 4...

fractional fluorescence change per unit activity	Required number of detected photons	
0.1%	16,000,000	
1%	160,000	
10%	1,600	
100%	16	

Required signal decreases with the square of the modulation!

Practical Implications

1- Increase the signal to noise ratio:

- optimize the excitation
- collect as many photons as possible
- decrease the noise to the shot-noise limit

2- Optimize the % of fluorescence modulation:

- avoid non-modulated signals (like tissue fluorescence or out-of focus fluorescence)

- resolve optically compartments with large signal dynamics







































How do you make filters?

See https://www.alluxa.com/learning-center/what-are-thin-film-optical-filters/

https://www.photonics.com/Articles/Thin-Film Optical Filters for Phase Control/a58006 https://www.photonics.com/Articles/Thin-Film_Coatings_A_Buyers_Guide/a42399

