Nature of Light Light can be described as a traveling electromagnetic wave

$$\begin{array}{l} \mathsf{E}\left(\mathsf{r},\mathsf{t}\right) \,=\, \mathsf{E}_{\mathsf{o}}\, {\rm sin}(\,\mathsf{k}\cdot\mathsf{x}\cdot\mathsf{w}\cdot\mathsf{w}\cdot\mathsf{t}+\varphi)\\ \\ \omega \,=\, 2\pi\cdot\mathsf{f} \qquad \text{angular frequency}\\ \\ \mathsf{f} \,=\, 1\,/\,\mathsf{T} \qquad \text{frequency}\\ \\ \mathsf{k} \,=\, 2\pi\,/\,\lambda \qquad \text{wave number} \end{array}$$



Light can be described as a traveling electromagnetic wave

$$E(\mathbf{r}, \mathbf{t}) = E_{o} \sin(\mathbf{k} \cdot \mathbf{x} - \omega \cdot \mathbf{t} + \phi)$$
  

$$\omega = 2\pi \cdot \mathbf{f} \quad \text{angular frequency}$$
  

$$\mathbf{f} = 1 / \mathbf{T} \quad \text{frequency}$$
  

$$\mathbf{k} = 2\pi / \lambda \quad \text{wave number}$$

which is a solution to the wave equation:

$$\frac{\partial^2 E}{\partial x^2} = \frac{1}{c^2} \frac{\partial^2 E}{\partial t^2}$$

 $F_{o}$  time  $F_{o}$  time  $F_{o}$  time  $F_{o}$  space c = speed of light in vacuum

$$c = f \cdot \lambda = \omega / k$$

 $I = Intensity = (c \cdot \varepsilon_0 \cdot n / 2) \cdot |E|^2$ 

Nature of Light Light can be described as a traveling electromagnetic wave

$$\begin{split} \mathsf{E}\left(\mathsf{r},\mathsf{t}\right) &= \mathsf{E}_{\mathsf{o}}\sin(\,\mathsf{k}\cdot\mathsf{x}\cdot\omega\cdot\mathsf{t}+\varphi)\\ & \omega &= 2\pi\cdot\mathsf{f} \qquad \text{angular frequency}\\ & \mathsf{f} &= 1\,/\,\mathsf{T} \qquad \text{frequency}\\ & \mathsf{k} &= 2\pi\,/\,\lambda \qquad \text{wave number} \end{split}$$





Single-slit diffraction pattern



Light can be described as an traveling electromagnetic wave





#### Double Slit Diffraction Experiment

Light can be described as discrete particles (photons)



#### Photoelectric Effect Albert Einstein, 1905 (Nobel Prize 1921) (Image taken from LLNL website)

Wave - Particle Duality



#### Photoelectric Effect Albert Einstein, 1905 (Nobel Prize 1921) (Image taken from LLNL website)



Young's Double Slit Experiment

# Light is an Electromagnetic Field

We will discuss electromagnetic fields in more detail when we cover Ch. 24



For now, the important point is that we can treat light as a transverse wave : as the light propogates forward, the electric field oscillates perpendicular to that direction of oscillation.

We will deal only with the electric field and completely ignore the magnetic field for now.

٠

 $\bullet$ 









#### Huygen's Principle:



#### Huygen's Principle:





#### Huygen's Principle:



#### Huygen's Principle:



#### Huygen's Principle:



#### Huygen's Principle:

Every point on a particular wavefront can be considered a "new source" of small spherical "wavelets".

As the wavelets propogate outward, the curve that runs tangent to these wavelets defines the new wavefront.



#### Huygen's Principle:

Every point on a particular wavefront can be considered a "new source" of small spherical "wavelets".

As the wavelets propogate outward, the curve that runs tangent to these wavelets defines the new wavefront.



#### Huygen's Principle:

Every point on a particular wavefront can be considered a "new source" of small spherical "wavelets".

As the wavelets propogate outward, the curve that runs tangent to these wavelets defines the new wavefront.

#### Note : A wavefront

is defined by the line (or curve) that connects the points of constant phase in a wave.



wavefront

example : a line through
the peaks of a set of sine waves



This may seem like a lot of effort to get a trivial result, but this same method will allows us to examine situations like diffraction andrefraction at an interface (Ch 25)

#### Huygen's Principle:

Every point on a particular wavefront can be considered a "new source" of small spherical "wavelets".

As the wavelets propogate outward, the curve that runs tangent to these wavelets defines the new wavefront.

#### Note : A wavefront

is defined by the line (or curve) that connects the points of constant phase in a wave.



wavefront

example : a line through
the peaks of a set of sine waves













Consider if we (somehow) have a wavefront that is completely straight? (We call this an "infinite plane wave" because in 3D space the straight wavefront is a giant flat sheet.

The tangent to the Huygen wavelets traces out another infinite plane wavefront.

Consider if we (somehow) have a wavefront that is completely straight? (We call this an "infinite plane wave" because in 3D space the straight wavefront is a giant flat sheet.

The tangent to the Huygen wavelets traces out another infinite plane wavefront.

How do we get an "infinite plane wave" to start with? Well, in reality we can never really get a truly infinite plane wave, but if we look at the light from a distant star, the radius of curvature of the wavefront is so large, that over any small area (say, this room), the wavefront appears flat, and seems to extend to infinity

# Diffraction



When we pass an [infinite] wave past a barrier (for example, through a hole) we break the symmetry of the Huygen wavelets near the edges.

As a result, waves diffract (bend) as they pass through small openings.

#### How small is small?

Diffraction becomes appreciable when the opening get to be approximately the same size or smaller than a wavelength of the wave passing through it.



Index of Refraction : 
$$n = \frac{\text{speed of light in vacuum}}{\text{speed of light in medium}} = \frac{c}{v}$$

# Huygen's Principle














#### **Approximations**

Brutalizing optics into 4 limiting regimes

- Ray (Geometric Optics) :  $\lambda \rightarrow 0$
- Paraxial Approximation :  $\theta \ll \pi/2$
- Thin Lens Approximation : lens thickness  $\rightarrow 0$
- Lossless Approximation : scatter, absorption  $\rightarrow 0$

# Ray Model / Geometric Optics

Assumes that (  $\lambda$  < d ) so that we can ignore diffraction effects

We will take our electromagnetic wave and strip it down to the ray (arrow) that points in the direction of the wave propogation.

The light rays are straight lines that are perpendicular to the wave fronts









When  $\lambda \ll d$ , the rays continue in a straight-line path and the ray approximation remains valid.



In the ray optics limit, we ignore diffraction.

# Rays : The Rules

- A geometric ray will move in a straight line as long as the medium does not change.
- When a geometric ray arrives at an interface between two different materials, it can reflect or refract to a new angle
- When dealing with interfaces, the angle of a geometric ray is always taken with respect to the "normal to the surface" (an imaginary line that is perpendicular to the surface)



#### Laws of Reflection and Refraction



Snell's Law :  $n_1 sin(\theta_1) = n_2 sin(\theta_2)$ 

Fermat's Principle Derivation : Principle of Least Time



What path should the lifeguard take to minimize the time to reach the drownng victim?



Fermat's Principle Derivation : Principle of Least Time



What path should the lifeguard take to minimize the time to reach the drownng victim?



Fermat's Principle Derivation : Principle of Least Time



What path should the lifeguard take to minimize the time to reach the drownng victim?





















One final (easy way) to think about (and remember) Snell's law

Consider a dumbell or car axle rolling on pavement at an angle towards a patch of of mud.

When the first wheel hits the mud, it slows down, but the other wheel is still on the fast pavement, and causes the trajectory of the axle to tilt towards the normal to the interface.














































Circularly Polarized Light





Circularly Polarized Light





















**High Performance Confocal Microscope Objective** 







Figure 1 Nosepiece Objective Threads Rear Aperture Manufacturer-ADO/ IR Barrel Objective Lens /120W Specifications-Mount Correction-Magnification Collar Triplet 0.11 0.14 0.17 0.20 0.23 Color Code, Lens Cover Group Immersion Color Code Glass

Thickness

Hemispherical

Lens Element

**Objective** 

Front Lens

Meniscus

Lens

High Performance Confocal Microscope Objective











+1)	Ē	LA1207	N-BK7 Plano-Convex Lens, Ø1/2", f = 10	0.0 mm, Uncoated	\$18.87
+1)=	=	LA1207-A	N-BK7 Plano-Convex Lens, Ø1/2", f = 10	0.0 mm, AR Coating: 350-700 nm	\$29.07
AR Coating Ran	nge		350 - 700 nm (-A Coating)		

AR Coating Range	350 - 700 nm (-A Coating)
Reflectance over Coating Range (Avg.)	<0.50%



AR Coating Range	350 - 700 nm (-A Coating)		
+1) 🖹 📕	<b>1207-A</b> N-BK7 Plano-Convex Lens, $\emptyset 1/2$ ", f = 10	00.0 mm, AR Coating: 350-700 nm	\$29.07
+1) 📄 🔛	<b>N-BK7</b> Plano-Convex Lens, $\emptyset 1/2^{"}$ , f = 10	00.0 mm, Uncoated	\$18.87

	· · · · · · · · · · · · · · · · · · ·	
Reflectance over	<0.50%	
Coating Range (Avg.)	<0.50%	



































## **Total Internal Reflection**







## **Total Internal Reflection**


#### **Total Internal Reflection**



#### **Total Internal Reflection**































#### THIS PAGE INTENTIONALLY LEFT BLANK (with the exception of the text declaring this page to be blank)

## **Approximations**

Brutalizing optics into 4 limiting regimes

- Ray (Geometric Optics) :  $\lambda \rightarrow 0$
- Paraxial Approximation :  $\theta \ll \pi/2$
- Thin Lens Approximation : lens thickness  $\rightarrow 0$
- Lossless Approximation : scatter, absorption  $\rightarrow 0$

















Gaussian Formulation :  $1/f = (1/d_1) + (1/d_2)$ 

Newtonian Formulation :  $f^2 = x_1 * x_2$ 

## Ray Tracing Rules : Real Images

Positive lens, Object outside the focal point



In: Parallel to optical axis In: Through front focal point In: Through center of lens







Positive lens, Object inisde the focal point



CSHL Imaging Course 2016







In: Parallel to optical axis In: Through front focal point In: Through center of lens



In: Parallel to optical axis In: Through front focal point In: Through center of lens



In: Parallel to optical axis In: Through front focal point In: Through center of lens


In: Parallel to optical axis In: Through front focal point In: Through center of lens Out: Through back focal point Out: Parallel to optical axis Out: Undeviated



In: Parallel to optical axis In: Through front focal point In: Through center of lens Out: Through back focal point Out: Parallel to optical axis Out: Undeviated



In: Through front focal point In: Through center of lens Out: Through back focal point Out: Parallel to optical axis Out: Undeviated



Human Observer



Human

Observer

























OBJECT VERY CLOSE TO LENS If we did not realize that there was a lens in the path, we would think that the light rays came from a point back here





OBJECT VERY CLOSE TO LENS

#### Imaging Conditions : d<sub>2</sub> vs d<sub>1</sub>



Image position (in focal lengths)